Lecture 13:
Memory Consistency
+ course-so-far review (if time)
Hello

Adele

(25)

Hello, it’s me
I was wondering if after all these lectures you’d like to meet
To go over everything
They say that studying’s supposed to help ya
But I ain’t done much studying

Hello, can you hear me
I’m in the library dreaming about what the exam is going to be
I hope it’s shorter, and covers ISPC
I’ve forgotten how it felt before I dealt with so much concurrency

“Adele, no one is going to understand your song about 418.” - Producers at XL Recordings
“Okay, fine… I’ll sing about nostalgia then.” - Adele
Today: what you should know

- Understand the motivation for relaxed consistency models
- Understand the implications of relaxing $W \rightarrow R$ ordering
Today: who should care

Anyone who:

- Wants to implement a synchronization library
- Will ever work a job in kernel (or driver) development
- Seeks to implement lock-free data structures *
- Does any of the above on ARM processors **

*    Topic of a later lecture
** For reasons to be described later
Memory coherence vs. memory consistency

- **Memory coherence** defines requirements for the observed behavior of reads and writes to the same memory location
  - All processors must agree on the order of reads/writes to X
  - In other words: it is possible to put all operations involving X on a timeline such that the observations of all processors are consistent with that timeline

- **Memory consistency** defines the behavior of reads and writes to different locations (as observed by other processors)
  - Coherence only guarantees that writes to address X will eventually propagate to other processors
  - Consistency deals with when writes to X propagate to other processors, relative to reads and writes to other addresses
Coherence vs. consistency
(said again, perhaps more intuitive this time)

- The goal of cache coherence is to ensure that the memory system in a parallel computer behaves as if the caches were not there
  - Just like how the memory system in a uni-processor system behaves as if the cache was not there

- A system without caches would have no need for cache coherence

- Memory consistency defines the allowed behavior of loads and stores to different addresses in a parallel system
  - The allowed behavior of memory should be specified whether or not caches are present (and that’s what a memory consistency model does)
Memory operation ordering

- A program defines a sequence of loads and stores (this is the “program order” of the loads and stores)

- Four types of memory operation orderings
  - \( W \rightarrow R \): write to \( X \) must commit before subsequent read from \( Y \) *
  - \( R \rightarrow R \): read from \( X \) must commit before subsequent read from \( Y \)
  - \( R \rightarrow W \): read to \( X \) must commit before subsequent write to \( Y \)
  - \( W \rightarrow W \): write to \( X \) must commit before subsequent write to \( Y \)

- A **sequentially consistent** memory system maintains all four memory operation orderings

* To clarify: “write must commit before subsequent read” means:
  When a write comes before a read in program order, the write must commit (its results are visible) by the time the read occurs.
Sequential consistency

- A parallel system is sequentially consistent if the result of any parallel execution is the same as if all the memory operations were executed in some sequential order, and the memory operations of any one processor are executed in program order.

There is a chronology of all memory operations that is consistent with observed values

- P0 store: X ← 5
- P1 store: X ← 10
- P0 store: Y ← 1
- P1 load: X
- P0 load: X
- P1 store: Y ← 20

Note, now timeline lists operations to addresses X and Y

[Adve and Gharachorloo 95]
Sequential consistency (switch metaphor)

- All processors issue loads and stores in program order
- Memory chooses a processor, performs a memory operation to completion, then chooses another processor, …
Quick example

Thread 1 (on P1)

\[
A = 1; \\
\text{if } (B == 0) \\
\text{print } \text{“Hello”};
\]

Thread 2 (on P2)

\[
B = 1; \\
\text{if } (A == 0) \\
\text{print } \text{“World”};
\]

Assume A and B are initialized to 0.

Question: Imagine threads 1 and 2 are being run simultaneously on a two processor system. What will get printed?

Answer: assuming writes propagate immediately (e.g., P1 won’t continue to ‘if’ statement until P2 observes the write to A), then code will either print “hello” or “world”, but not both.
Consider various interleavings...

Thread 1 (on P1)
A = 1;
if (B == 0)
   print “Hello”;

Thread 2 (on P2)
B = 1;
if (A == 0)
   print “World”;

P1: Write 1 to A
P1: Read B (it’s 0, print “Hello”)
P2: Write 1 to B
P2: Read A (it’s 1)

P2: Write 1 to B
P2: Read A (it’s 0, print “World”)
P1: Write 1 to A
P1: Read B (it’s 1)

P2: Write 1 to B
P2: Read A (it’s 1)
P1: Write 1 to A
P1: Read B (it’s 1)

P1: Write 1 to A
P2: Write 1 to B
P2: Read A (it’s 1)
P1: Read B (it’s 1)

Answer: assuming writes propagate immediately (e.g., P1 won’t continue to ‘if’ statement until P2 observes the write to A), then code will either print “hello” or “world”, but not both.
Relaxing memory operation ordering

- A **sequentially consistent** memory system maintains all four memory operation orderings \((W \rightarrow R, R \rightarrow R, R \rightarrow W, W \rightarrow W)\)

- Relaxed memory consistency models allow certain orderings to be violated
Back to the quick example

Thread 1 (on P1)

\[
A = 1; \\
\text{if } (B == 0) \\
\text{print "Hello";}
\]

From the processor’s perspective, these are independent instructions in each thread.

Thread 2 (on P2)

\[
B = 1; \\
\text{if } (A == 0) \\
\text{print "World";}
\]

(If this was a sequential program, it would not violate program correctness if a processor chose to reorder them... e.g., execute them concurrently)
Motivation for relaxed consistency: hiding latency

Why are we interested in relaxing ordering requirements?
- To gain performance
- Specifically, hiding memory latency: overlap memory access operations with other operations when they are independent
- Remember, memory access in a cache coherent system may entail much more work than simply reading bits from memory (finding data, sending invalidations, etc.)
Another way of thinking about relaxed ordering

<table>
<thead>
<tr>
<th>Program order</th>
<th>“Sufficient” order for correctness</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thread 1 (on P1)</td>
<td>Thread 2 (on P2)</td>
</tr>
<tr>
<td>A = 1;</td>
<td>A = 1;</td>
</tr>
<tr>
<td>B = 1;</td>
<td>B = 1;</td>
</tr>
<tr>
<td>unlock(L);</td>
<td>unlock(L);</td>
</tr>
<tr>
<td>lock(L);</td>
<td>lock(L);</td>
</tr>
<tr>
<td>x = A;</td>
<td>x = A;</td>
</tr>
<tr>
<td>y = B;</td>
<td>y = B;</td>
</tr>
</tbody>
</table>

An intuitive notion of correct = execution produces the same results as a sequentially consistent system
Allowing reads to move ahead of writes

- Four types of memory operation orderings
  - $W \rightarrow R$: write must complete before subsequent read
  - $R \rightarrow R$: read must complete before subsequent read
  - $R \rightarrow W$: read must complete before subsequent write
  - $W \rightarrow W$: write must complete before subsequent write

- Allow processor to hide latency of writes
  - Total Store Ordering (TSO)
  - Processor Consistency (PC)
Write buffering example

- **Write buffering** is a common processor optimization that allows reads to proceed in front of prior writes
  - When store is issued, processor buffers store in write buffer (assume store is to address X)
  - Processor immediately begins executing subsequent loads, provided they are not accessing address X (exploits ILP in program)
  - Further writes can also be added to write buffer (write buffer is processed in order, there is no $W \rightarrow W$ reordering)

- **Write buffering** relaxes $W \rightarrow R$ ordering

---

*Do not confuse a write buffer (shown here) with a cache’s write-back buffer (discussed last lecture). Both buffers exist to hide the latency of memory operations. However, the write buffer holds writes that have been issued by the processor, but not yet committed in the system. The write-back buffer holds dirty cache lines that must be flushed to memory so memory stays up to date. The lines are dirty because there was some write to them completed by the processor a long time ago. (This is a good distinction to discuss in comments.)*
Relaxed consistency performance

**Base**: Sequentially consistent execution. Processor issues one memory operation at a time, stalls until completion

**W-R**: relaxed $W \rightarrow R$ ordering constraint (write latency almost fully hidden)
Allowing reads to move ahead of writes

- **Total store ordering (TSO)**
  - Processor P can read B before its write to A is seen by all processors (processor can move its own reads in front of its own writes)
  - Reads by other processors cannot return new value of A until the write to A is observed by all processors

- **Processor consistency (PC)**
  - Any processor can read new value of A before the write is observed by all processors

- In TSO and PC, only W→R order is relaxed. The W→W constraint still exists. Writes by the same thread are not reordered (they occur in program order)
Four example programs

1. Thread 1 (on P1)
   A = 1;
   flag = 1;

   Thread 2 (on P2)
   while (flag == 0);
   print A;

2. Thread 1 (on P1)
   A = 1;
   B = 1;

   Thread 2 (on P2)
   print B;
   print A;

3. Thread 1 (on P1)
   A = 1;
   while (A == 0);
   B = 1;

   Thread 2 (on P2)
   while (A == 0);
   B = 1;
   print A;

4. Thread 1 (on P1)
   A = 1;
   B = 1;

   Thread 2 (on P2)
   B = 1;
   print A;

Assume A and B are initialized to 0
Assume prints are loads

Do results of execution match that of sequential consistency (SC)

<table>
<thead>
<tr>
<th></th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total Store Ordering (TSO)</td>
<td>✔</td>
<td>✔</td>
<td>✔</td>
<td>✗</td>
</tr>
<tr>
<td>Processor Consistency (PC)</td>
<td>✔</td>
<td>✔</td>
<td>✗</td>
<td>✗</td>
</tr>
</tbody>
</table>
Clarification

- The cache coherency problem exists because of the optimization of duplicating data in multiple processor caches. The copies of the data must be kept coherent.

- Relaxed memory consistency issues arise from the optimization of reordering memory operations. (Consistency is unrelated to whether or not caches exist in the system.)
Allowing writes to be reordered

Four types of memory operation orderings
- $W \rightarrow R$: write must complete before subsequent read
- $R \rightarrow R$: read must complete before subsequent read
- $R \rightarrow W$: read must complete before subsequent write
- $W \rightarrow W$: write must complete before subsequent write

Partial Store Ordering (PSO)
- Execution may not match sequential consistency on program 1
  (P2 may observe change to $\text{flag}$ before change to $A$

Thread 1 (on P1)
$A = 1;$
$\text{flag} = 1;$

Thread 2 (on P2)
while ($\text{flag} == 0$);
print $A;$
Why might it be useful to allow more aggressive memory operation reorderings?

- **W → W**: processor might reorder write operations in a write buffer (e.g., one is a cache miss while the other is a hit)

- **R → W, R → R**: processor might reorder independent instructions in an instruction stream (out-of-order execution)

- Keep in mind these are all valid optimizations if a program consists of a single instruction stream
Allowing all reorderings

- **Four types of memory operation orderings**
  - $W \rightarrow R$: write must complete before subsequent read
  - $R \rightarrow R$: read must complete before subsequent read
  - $R \rightarrow W$: read must complete before subsequent write
  - $W \rightarrow W$: write must complete before subsequent write

- **Examples:**
  - Weak ordering (WO)
  - Release Consistency (RC)
    - Processors support special synchronization operations
    - Memory accesses before memory fence instruction must complete before the fence issues
    - Memory accesses after fence cannot begin until fence instruction is complete
Example: expressing synchronization in relaxed models

- Intel x86/x64 ~ total store ordering
  - Provides sync instructions if software requires a specific instruction ordering not guaranteed by the consistency model
    - `mm_lfence` ("load fence": wait for all loads to complete)
    - `mm_sfence` ("store fence": wait for all stores to complete)
    - `mm_mfence` ("mem fence": wait for all me operations to complete)

- ARM processors: very relaxed consistency model

A cool post on the role of memory fences in x86:
http://bartoszmilewski.com/2008/11/05/who-ordered-memory-fences-on-an-x86/

ARM has some great examples in their programmer’s reference:

A great list:
http://www.cl.cam.ac.uk/~pes20/weakmemory/
Acquire/release semantics

- Operation X with acquire semantics: prevent reordering of X with any load/store after X in program order
  - Other processors see X’s effect before the effect of all subsequent operations
  - Example: taking a lock must have acquire semantics

- Operation X with release semantics: prevent reordering of X with any load/store before X in program order
  - Other processors see effects of all prior operations before seeing effect of X.
  - Example: releasing a lock must have release semantics
C++ 11 atomic<T>

- Provides atomic read, write, read-modify-write of entire objects
  - Atomicity may be implemented by mutex or efficiently by processor-supported atomic instructions (if T is a basic type)
  - More on this after spring break

- Provides memory ordering semantics for operations before and after atomic operations
  - By default: sequential consistency
  - See std::memory_order or more detail

```c++
// other code...
while (ready.load()==0);
// use foo here...
```

C++ atomic ensures sequentially consistent behavior by default, so compiler must emit appropriate fences on x86
C++ 11 atomic<T>

- Provides atomic read, write, read-modify-write of entire objects
  - Atomicity may be implemented by mutex or efficiently by processor-supported atomic instructions (if T is a basic type)
  - More on this after spring break

- Provides memory ordering semantics for operations before and after atomic operations
  - By default: sequential consistency
  - See std::memory_order or more detail

```c++
// other code...
while (ready.load(memory_order_acquire) == 0);
// use foo here...
```

No fence required on x86
Conflicting data accesses

- Two memory accesses by different processors conflict if…
  - They access the same memory location
  - At least one is a write

- Unsynchronized program
  - Conflicting accesses not ordered by synchronization (e.g., a fence, operation with release/acquire semantics, barrier, etc.)
  - Unsynchronized programs contain data races: the output of the program depends on relative speed of processors (non-deterministic program results)
Synchronized programs

- Synchronized programs yield SC results on non-SC systems
  - Synchronized programs are data-race-free

- In practice, most programs you encounter will be synchronized (via locks, barriers, etc. implemented in synchronization libraries)
  - Rather than via ad-hoc reads/writes to shared variables like in the earlier “four example programs” slide
Summary: relaxed consistency

- **Motivation:** obtain higher performance by allowing recording of memory operations (reordering is not allowed by sequential consistency)

- **One cost is software complexity:** programmer or compiler must correctly insert synchronization to ensure certain specific operation orderings when needed
  - But in practice complexities encapsulated in libraries that provide intuitive primitives like lock/unlock, barrier (or lower level primitives like fence)
  - Optimize for the common case: most memory accesses are not conflicting, so don’t design a system that pays the cost as if they are

- **Relaxed consistency models differ in which memory ordering constraints they ignore**
Eventual consistency in distributed systems

- For many of you, relaxed memory consistency will be a key factor in writing web-scale programs in distributed environments

- "Eventual consistency"
  - Say machine A writes to an object X in a shared distributed database
  - Many copies of database exist for performance scaling and redundancy
  - Eventual consistency guarantees that if there are no other updates to X, A’s update will eventually be observed by all other nodes in the system (note: no guarantees on when, so updates to objects X and Y might propagate to different clients differently)

Post to Facebook wall: "Woot! The 418 exam is gonna be great!"
If time: course so far review
(a more-or-less randomly selected collection of topics from previous lectures)
Exam details

- Closed book, closed laptop
- One “post it” note (but we’ll let you use both sides)
- Covers all lecture material so far in course, including today’s discussion of memory consistency
- The TAs will lead a review session on Monday at 6:30 in Rashid
  - Please come with questions
Throughput vs. latency

**THROUGHPUT**
The rate at which work gets done.
- Operations per second
- Bytes per second (bandwidth)
- Tasks per hour

**LATENCY**
The amount of time for an operation to complete
- An instruction takes 4 clocks
- A cache miss takes 200 clocks to complete
- It takes 20 seconds for a program to complete
Ubiquitous parallelism

What motivated the shift toward multi-core parallelism in modern processor design?

- Inability to scale clock frequency due to power limits
- Diminishing returns when trying to further exploit ILP

Is the new performance focus on throughput, or latency?
# Techniques for exploiting independent operations in applications

<table>
<thead>
<tr>
<th></th>
<th>What is it? What is the benefit?</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>1. superscalar</strong></td>
<td>Processor executes multiple instructions per clock. Super-scalar execution exploits instruction level parallelism (ILP). When instructions in the same thread of control are independent they can be executed in parallel on a super-scalar processor.</td>
</tr>
<tr>
<td><strong>execution</strong></td>
<td></td>
</tr>
<tr>
<td><strong>2. SIMD</strong></td>
<td>Processor executes the same instruction on multiple pieces of data at once (e.g., one operation on vector registers). The cost of fetching and decoding the instruction is amortized over many arithmetic operations.</td>
</tr>
<tr>
<td><strong>execution</strong></td>
<td></td>
</tr>
<tr>
<td><strong>3. multi-core</strong></td>
<td>A chip contains multiple (mainly) independent processing cores, each capable of executing independent instruction streams.</td>
</tr>
<tr>
<td><strong>execution</strong></td>
<td></td>
</tr>
<tr>
<td><strong>4. multi-threaded</strong></td>
<td>Processor maintains execution contexts (state: e.g., a PC, registers, virtual memory mappings) for multiple threads. Execution of thread instructions is interleaved on the core over time. Multi-threading reduces processor stalls by automatically switching to execute other threads when one thread is blocked waiting for a long-latency operation to complete.</td>
</tr>
<tr>
<td><strong>execution</strong></td>
<td></td>
</tr>
<tr>
<td>Techniques for exploiting independent operations in applications</td>
<td>Who is responsible for mapping?</td>
</tr>
<tr>
<td>---------------------------------------------------------------</td>
<td>---------------------------------</td>
</tr>
<tr>
<td>1. superscalar execution</td>
<td>Usually not a programmer responsibility: ILP automatically detected by processor hardware or by compiler (or both) (But manual loop unrolling by a programmer can help)</td>
</tr>
<tr>
<td>2. SIMD execution</td>
<td>In simple cases, data parallelism is automatically detected by the compiler, (e.g., assignment 1 saxpy). In practice, programmer explicitly describes SIMD execution using vector instructions or by specifying independent execution in a high-level language (e.g., ISPC gangs, CUDA)</td>
</tr>
<tr>
<td>3. multi-core execution</td>
<td>Programmer defines independent threads of control. e.g., pthreads, ISPC tasks, openMP #pragma</td>
</tr>
<tr>
<td>4. multi-threaded execution</td>
<td>Programmer defines independent threads of control. But programmer must create more threads than processing cores.</td>
</tr>
</tbody>
</table>
Frequently discussed processor examples

- **Intel Core i7 CPU**
  - 4 cores
  - Each core:
    - Supports 2 threads ("Hyper-Threading")
    - Can issue 8-wide SIMD instructions (AVX instructions) or 4-wide SIMD instructions (SSE)
    - Can execute multiple instructions per clock (superscalar)

- **NVIDIA GTX 1080 GPU**
  - 20 “SM cores”
  - Each core:
    - Supports up to 64 warps (warp is a group of 32 “CUDA threads”)
    - Issues 32-wide SIMD instructions (same instruction for all 32 “CUDA threads” in a warp)
    - Also capable of issuing multiple instructions per clock

- **Intel Xeon Phi (KNL)**
  - 72 cores
  - Each core: supports 4 threads, 16-wide SIMD instructions
  - Also capable of multiple instructions per clock (up to 2 SIMD instructions)
Multi-threaded, SIMD execution on GPU

- Registers for warp execution contexts: max 64 (256 KB)
- "Shared" memory storage (96 KB)
- L1 cache (48 KB)

SM resource limits:
- Max warp execution contexts: 64 (2,048 total CUDA threads)
- 96 KB of shared memory

Describe how CUDA threads are mapped to the execution resources on this GTX 1080 GPU SM?
- e.g., describe how the processor executes instructions each clock
You used ISPC to parallelize the Mandelbrot generation

You created a bunch of tasks. How many? Why?

```c
uniform int rowsPerTask = height / 2;

// create a bunch of tasks

launch[2] mandelbrot_ispc_task(
    x0, y0, x1, y1,
    width, height,
    rowsPerTask,
    maxIterations,
    output);
```
Amdahl’s law

- Let $S =$ the fraction of sequential execution that is inherently sequential
- Max speedup on $P$ processors given by:

$$\text{speedup} \leq \frac{1}{S + \frac{1 - S}{P}}$$
Thought experiment

- Your boss gives your team a piece of code for which 25% of the operations are inherently serial and instructs you to parallelize the application on a six-core machine. He expects you to achieve 5x speedup on this application.

- Your friend shouts at your boss, “that is %#$*$(!@ impossible”!

- Your boss shouts back, “I want employees with a can-do attitude! You haven’t thought hard enough.”

- Who is right?
Work assignment

Problem to solve

Subproblems ("tasks")

Threads (or processors)

Static Assignment

Assignment of subproblems to processors is determined before (or right at the start) of execution. Assignment does not depend on execution behavior.

Good: very low (almost none) run-time overhead
Bad: execution time of subproblems must be predictable (so programmer can statically balance load)

Examples: solver kernel, OCEAN, mandlebrot in asst 1, problem 1, ISPC foreach

Dynamic Assignment

Assignment of subproblems to processors is determined as the program runs.

Good: can achieve balance load under unpredictable conditions
Bad: incurs runtime overhead to determine assignment

Examples: ISPC tasks, executing grid of CUDA thread blocks on GPU, assignment 3, shared work queue
Balancing the workload

Ideally all processors are computing all the time during program execution (they are computing simultaneously, and they finish their portion of the work at the same time).

Load imbalance can significantly reduce overall speedup.
Dynamic assignment using work queues

Sub-problems (aka “tasks”, “work”)

Shared work queue: a list of work to do (for now, let’s assume each piece of work is independent)

Worker threads:
Pull data from work queue
Push new work to queue as it’s created
Decomposition in assignment 2

- Most solutions decomposed the problem in several ways
  - Decomposed screen into tiles ("task" per tile)
    - Decomposed tile into per circle "tasks"
    - Decomposed tile into per pixel "tasks"
Artifactual vs. inherent communication

INHERENT COMMUNICATION

ARTIFACTUAL COMMUNICATION

FALSE SHARING

Problem assignment as shown. Each processor reads/writes only from its local data.
# Programming model abstractions

<table>
<thead>
<tr>
<th></th>
<th>Structure?</th>
<th>Communication?</th>
<th>Sync?</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. shared</td>
<td>Multiple processors sharing an address space.</td>
<td>Implicit: loads and stores to</td>
<td>Synchronization primitives such as locks and barriers</td>
</tr>
<tr>
<td>address space</td>
<td></td>
<td>shared variables</td>
<td></td>
</tr>
<tr>
<td>2. message</td>
<td>Multiple processors, each with own memory</td>
<td>Explicit: send and receive</td>
<td>Build synchronization out of messages.</td>
</tr>
<tr>
<td>passing</td>
<td>address space.</td>
<td>messages</td>
<td></td>
</tr>
<tr>
<td>3. data-parallel</td>
<td>Rigid program structure: single logical</td>
<td>Typically not allowed within map</td>
<td>Implicit barrier at the beginning and end of the map.</td>
</tr>
<tr>
<td></td>
<td>thread containing map(f, collection) where</td>
<td>except through special built-in</td>
<td></td>
</tr>
<tr>
<td></td>
<td>“iterations” of the map can be executed</td>
<td>primitives (like “reduce”). Comm</td>
<td></td>
</tr>
<tr>
<td></td>
<td>concurrently</td>
<td>implicit through loads and stores to address space</td>
<td></td>
</tr>
</tbody>
</table>
Cache coherence

Why cache coherence?
Hand-wavy answer: would like shared memory to behave “intuitively” when two processors read and write to a shared variable. Reading a value after another processor writes to it should return the new value. (despite replication due to caches)

Requirements of a coherent address space

1. A read by processor P to address X that follows a write by P to address X, should return the value of the write by P (assuming no other processor wrote to X in between)

2. A read by a processor to address X that follows a write by another processor to X returns the written value... if the read and write are sufficiently separated in time (assuming no other write to X occurs in between)

3. Writes to the same location are serialized; two writes to the same location by any two processors are seen in the same order by all processors.
   (Example: if values 1 and then 2 are written to address X, no processor observes 2 before 1)

Condition 1: program order (as expected of a uniprocessor system)

Condition 2: write propagation: The news of the write has to eventually get to the other processors. Note that precisely when it is propagated is not defined by definition of coherence.

Condition 3: write serialization
Implementing cache coherence

Main idea of invalidation-based protocols: before writing to a cache line, obtain exclusive access to it

**SNOOPING**

Each cache broadcasts its cache misses to all other caches. Waits for other caches to react before continuing.

*Good*: simple, low latency
*Bad*: broadcast traffic limits scalability

**DIRECTORIES**

Information about location of cache line and number of shares is stored in a centralized location. On a miss, requesting cache queries the directory to find sharers and communicates with these nodes using point-to-point messages.

*Good*: coherence traffic scales with number of sharers, and number of sharers is usually low
*Bad*: higher complexity, overhead of directory storage, additional latency due to longer critical path
MSI state transition diagram

- **M (Modified)**
  - PrRd / --
  - PrWr / --
  - PrWr / BusRdX
  - PrRd / BusRd

- **S (Shared)**
  - PrRd / BusRd
  - PrWr / BusRdX

- **I (Invalid)**
  - PrRd / BusRd
  - PrWr / BusRdX

- **Broadcast (bus) initiated transaction**
  - BusRd / flush
  - BusRdX / flush

- **Processor initiated transaction**
  - A / B: if action A is observed by cache controller, action B is taken

- **PrRd / --**
- **PrWr / --**
- **PrWr / BusRdX**
- **PrRd / BusRd**
- **BusRd / flush**
- **BusRdX / flush**
- **BusRdX / --**